J. Rostand, On the automorphisms of the spectral unit ball, *Studia Math.*, 155:3 (2003), 207–230

Abstract

Let Ω be the spectral unit ball of $M_n(\mathbf{C})$, that is, the set of $n \times n$ matrices with spectral radius less than 1. We are interested in classifying the automorphisms of Ω . We know that it is enough to consider the normalized automorphisms of Ω , that is the automorphisms F satisfying F(0) = 0 and F'(0) = I, where I is the identity map on $M_n(\mathbf{C})$. The known normalized automorphisms are conjugations. Is every normalized automorphism a conjugation? We show that locally, in a neighborhood of a matrix with distinct eigenvalues, the answer is yes. We also prove that a normalized automorphism of Ω is a conjugation almost everywhere on Ω .