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## Abstract

Let  $\mathcal{A} = l^1(\mathbf{Z}_+)$  be the unital semigroup algebra of  $\mathbf{N}$ . We show that the cyclic cohomology groups  $\mathcal{H}C^n(\mathcal{A},\mathcal{A}')$  vanish when n is odd and are one-dimensional when n is even  $(n \geq 2)$ . Using Connes' exact sequence, these results are used to show that the simplicial cohomology groups  $\mathcal{H}^n(\mathcal{A},\mathcal{A}')$  vanish for  $n \geq 2$ . The results obtained are extended to unital algebras  $l^1(S)$  for some other semigroups of  $\mathbf{R}$ .